Efficient Coupled Electromagnetic-Thermal Induction Machine Model using scaled FE-Solutions

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*Abstract***—Coupled electromagnetic-thermal models are beneficial to simulate the thermal, electromagnetic loss-dependent behavior of machines. Coupling detailed thermal network models and electromagnetic finite element simulation results in high computation time. In this paper a scaling procedure is used to scale the solutions of a in beforehand simulated finite element solution coupled to an analytic three node thermal network model. This approach enables an efficient calculation of the machine temperature considering temperature dependent losses.**

*Index Terms***—induction machine, thermal model, scaling laws, finite element simulation**

I. Introduction

Since the heating of an induction machine (IM) depends on the electromagnetic losses the magnetic and the thermal analysis have to be coupled in the design process [1]. In [2] an analytic thermal network model is coupled to an finite-element (FE)-simulation, where the electric conductivities are updated. In [3] a thermal network model is coupled with an electromagnetic model in the stator reference frame based on the flux-linkage equations and the two axis theory. In [1] an analytic thermal and electromagnetic model, which is parametrized by FE-simulation data, is used to realize the thermal-electromagnetic coupling. In this paper an analytic three node thermal network model is coupled with a scaling procedure enabling a rapid calculation using FE-simulation data. This scaling procedure allows the possibility to scale the solutions, particularly the losses, of a beforehand performed FEsimulation.

II. Thermal Model of the Induction Machine

To simulate the thermal behavior of an IM the thermal three node network model in Fig. 1 is used, which inputs

Figure 1: Thermal Three Node Model of the IM.

are the FE calculated rotor losses $P_{L,r}$, the stator ohmic losses *P*L*,*ohm*,*^s and the stator iron losses *P*L*,*Fe*,*s. Node one presents the rotor including the shaft, rotor cage and bearings, node two the stator winding and node three the stator lamination including the housing of the machine.

For the parametrization of the thermal model analytic calculations and an Evolutionary Strategy as described in [4] are applied. The thermal air gap resistance R_δ is calculated according to the approach in [5]. The heat capacity of the stator winding $C_{s,Cu}$ is calculated by using the mass of the copper winding and its specific thermal capacity. For the heat transfer coefficient from the winding to the stator iron $\alpha_{\rm s, Cu-Fe}$ and from the stator iron to the ambient $\alpha_{\rm s, Fe-Amb}$ lower and upper limits, shown in table I, according to [5] and [6] are used. The lower and upper limits of the heat capacity of the rotor *C*^r results from a calculation with a tolerance of $\pm 10\%$ of the calculated data. The lower limit of the heat capacity of the stator iron $C_{s,Fe}$ is calculated by considering only the stator lamination and the upper limit by considering the stator lamination, the housing and the bearing shields. The optimization is carried out on the basis of four measurements and the measured temperatures after 30 min. The torque and speed as well as the measured winding and rotor cage temperature are listed in table II for various operation points. The resulting rotor and winding temperature of the optimization are also listed in table II and show a sufficiently accurate result for the calculations presented here. The resulting data of the parameterization are listed in table I.

Table I: Boundary conditions and results of parameter identification.

Variable	Unit	Lower Limit	Upper Limit	Calculated Data
	kJ/K	5.51	6.73	6.71
$C_{\rm s,Fe}$	kJ/K	11.78	13.6	13.2
$\alpha_{\rm s.Fe-Amb}$	$\mathrm{W/(m^2\,K)}$	25	250	60.94
$\alpha_{\rm s,Cu-Fe}$	$\mathrm{W/(m^2\,K)}$	10	100	74.75

Table II: Derivation of temperatures in measurement and simulation.

III. Scaling Laws of Induction Machines

In [7] an approach to scale the FE solutions of IMs considering geometric variations as well as variations in temperature is proposed. This scaling approach is used in this paper to show the influence of temperature variations in the simulation of IMs.

A. Temperature Scaling of the Stator Resistance

The stator resistance is evaluated in the post processing routine of an IM FE simulation. Therefore, temperature changes in the stator winding can be considered by recalculating the stator resistance R_s using (1). Here, α is the temperature coefficient of the stator winding material, $\vartheta_{\text{sim,new}}$ the new simulated stator temperature and ϑ_{ref} the reference temperature. The scaled stator resistance $R_{\rm s}^{'}$ leads to scaled Ohmic losses of the stator $P'_{\text{L,ohm,s}}$ in (2) that are used in the thermal model of the IM of Fig. 1.

$$
R_{\rm s}^{'} = R_{\rm s} \cdot \left(1 + \alpha \left(\vartheta_{\rm sim, new} - \vartheta_{\rm ref} \right) \right) \tag{1}
$$

$$
P^{'}_{\mathrm{L,ohm,s}} = 3 \cdot {I_{\mathrm{s}}}^2 \cdot R^{'}_{\mathrm{s}} \qquad \qquad (2)
$$

B. Temperature Scaling of the Rotor Resistance

In contrast to the stator resistance the rotor resistance R_r is defined in the preprocessing of the FE simulation in the form of a compensating conductivity as described in [7]. The temperature variation of the rotor cage and rotor conductivity respectively can be considered by the second rotor resistance scaling factor k_{R2} introduced in [7]. It is dependent on the old and new conductivity, $\sigma_{\rm r}$ and σ _{r,new}, the old and new temperature coefficients α and α_{new} , the old and new reference temperatures ϑ_{ref} and $\vartheta_{\text{ref,new}}$ and the old and new simulation temperatures ϑ_{sim} and $\vartheta_{\rm sim,new}.$

$$
k_{R2} = \frac{\sigma_r}{\sigma_{r,new}} \frac{1 + \alpha_{new} \left(\vartheta_{sim,new} - \vartheta_{ref,new}\right)}{1 + \alpha \left(\vartheta_{sim} - \vartheta_{ref}\right)} \tag{3}
$$

By neglecting the other scaling possibilities in [7], such as geometric scaling, the temperature change in the rotor cage yields the scaled rotor resistance:

$$
R_{\rm r}^{'} = R_{\rm r} \cdot k_{\rm R2} \tag{4}
$$

and to the scaled Ohmic losses of the rotor $P'_{\text{L,ohm,r}}$:

$$
P'_{\text{L},\text{ohm},\text{r}} = P_{\text{L},\text{ohm},\text{r}} \cdot k_{\text{R2}},\tag{5}
$$

that are used in the thermal model of the IM of Fig. 1.

IV. Calculation of Induction Machines considering temperature changes

With the parametrized thermal three node model of the IM a continuous operation of the machine with a torque of $T = 56$ N m and a speed of $n = 3700$ rpm is simulated once without a rescaling of the Ohmic losses in the stator and rotor due to a temperature change and once with rescaling the Ohmic losses of the machine. The results

Figure 2: Results of the Temperature Simulation with (w) and without (w/o) rescaling of the IM.

in Fig. 2 show that the consideration of the temperature variations have a high influence on the thermal behavior of the IM. The simulation with scaled machine achieves a lower temperature in the first 1500s and a much higher temperature after 1500 s.

V. Conclusions and Further Work

In this paper a parametrized analytic thermal three node network model of an IM is proposed. Furthermore, the scaling laws of an IM are used to scale the FE solutions due to temperature variations in the stator and rotor of the machine. A thermal simulation with and without using the presented scaling approach shows a high influence on the simulated thermal behavior of the IM considering temperature scaled machine losses or not. The full paper will present more detailed descriptions of the thermal model, the scaling procedure and the influence of the temperature consideration in the thermal simulation. It will also emphasize the rapid calculation of the method.

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