

# Automated Sizing of Permanent Magnet Synchronous Machines with respect to Electromagnetic and Thermal Aspects

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**Abstract**—The design of modern high power density permanent magnet synchronous machines requires adapted automated design tools. The temperature estimation at characteristic points of the machine, and in particular in permanent magnets, is essential to accurately simulate the electromagnetic behavior and avoid irreversible demagnetization. In this paper, an electromagnetic dimensioning model, parameterized by FEA, is coupled to a thermal lumped-parameter model to constitute a fast and efficient design tool for electrical machines. On two standard industrial servo-motors the whole design process, including sizing, electromagnetic and thermal modeling is applied and discussed.

## I. INTRODUCTION

**E**SPECIALLY in case of high power density permanent magnet synchronous machines (PMSM), the design process is challenged by modeling the machine's internal thermal behavior. The temperature dependency of the permanent magnet remanence flux density strongly influences the results of the electromagnetic simulation. Moreover, even in worst case of the ambient temperature, winding and magnet temperature have to remain below their maximum temperature limit to prevent irreversible material damage. Therefore thermal aspects have to be considered as an important part of the electromagnetic design process. Performing a thermal finite element analysis (FEA) for each design candidate of the machine is very time-consuming and not acceptable at early design stages. In this paper, a lumped-parameter thermal model is coupled with the electromagnetic model presented in [1] to allow thermal analysis as part of an automated sizing and design process. Finally the results of the coupled approach are compared with electrical and thermal measurements of two standard industrial servo-motors.

## II. AUTOMATED DESIGN PROCESS

The software presented in this paper is specialized in the rapid-prototype development of electrical machines [2]. Initially, a rough dimensioning on basis of classical design parameters such as rated torque, speed and voltage is

performed. Then a parameterized and hybrid FE-analytical electromagnetic model [1], which combines analytical and numerical advantages, is applied to archive fast and accurate electromagnetic simulation results. The computed losses are automatically introduced as heat sources in the thermal model. A post-processing layer monitors the deviation between results and predefined requirements after each calculation. If necessary, a feedback loop for optimization is initialized. Finally the optimum machine design can be analyzed accurately by thermal FEA. The FEA is done with the iMOOSE package [3],[4], all other computations are based on Python [5] and the scientific python extension [6].

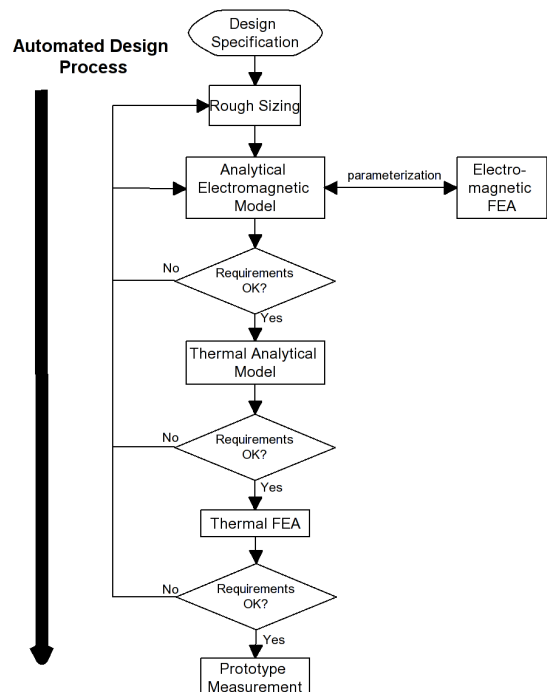


Fig. 1. Flowchart of automated design process for permanent magnet synchronous machines.

### III. THERMAL ANALYTICAL MODEL

Lumped-parameter thermal models have shown to be effective in estimating the temperatures at critical locations in electrical machines. The approach is characterized by a short computation time and a good adaptability to empirical or knowledge based data, although a minor loss of accuracy and detail can be observed in comparison to thermal FEA. This paper presents a modified version of the thermal lumped-parameter model presented in [7], where a water-cooled surface mounted permanent magnet synchronous machine for a hybrid electric vehicle has been analyzed in steady-state and transient simulation assuming a constant reference temperature at the frame. The eight-node thermal equivalent circuit model of [7] is shown in Fig. 2. Each node represents a specific machine part. The thermal resistances between the nodes represent the motor's three-dimensional heat flow, considering material properties as well as the complex air gap and end winding convection behavior. The model has proved very flexible; [8] presents an adaptation of this model for internal permanent magnet synchronous machines. Losses of

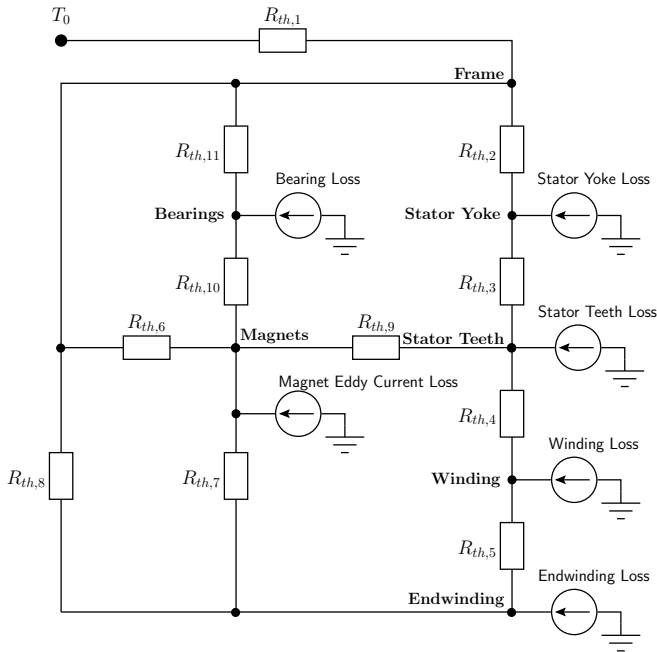


Fig. 2. Thermal network model of a passive cooled surface mounted PMSM.

electromagnetic origin, in stator teeth, stator yoke, winding or end winding, are represented by equivalent currents injected into the network to determine the corresponding temperature rise (voltage) of each specific part with respect to  $T_0$ . Lindström's simplification assuming an isothermal constant temperature around the frame ( $T_0$ ) is replaced by modeling the heat transfer between frame and ambient air. In case of passive cooling, the frame temperature is a nonlinear function

of the motor's radiation and convection properties. Before solving the network equations of Fig. 2, the corresponding frame temperature  $T_0$  has to be determined.

Newton's Law, governing the heat convection, states:

$$Q_{con} = Ah(T_0 - T_\infty) \quad , \quad (1)$$

where  $Q_{con}$  is the power transferred by convection,  $A$  the involved frame surface,  $h$  an empirical convection coefficient,  $T_0$  the average frame temperature and  $T_\infty$  the ambient air temperature. According to [9] the heat transfer coefficient  $h$  around horizontally mounted cylinder can be estimated by

$$h = \frac{Nu \cdot \lambda}{l} \quad (2)$$

$$= \frac{\lambda}{l} \{0.752 + 0.387 \sqrt[3]{Gr \cdot Pr \cdot f_3(Pr)}\} \quad (3)$$

$$Pr = \frac{\eta \cdot c_p}{\lambda} \quad (4)$$

$$Gr = \frac{g \cdot (T_0 - T_\infty) \cdot l^3}{T_\infty \nu^2} \quad (5)$$

$$f_3(Pr) = \left[ 1 + \left( \frac{0.559}{Pr} \right)^{\frac{9}{16}} \right]^{\frac{-16}{9}} \quad (6)$$

$h$  depends on the characteristic length  $l$ , the thermal conductivity  $\lambda$  and the Nusselt number  $Nu$ , which is a function of Grashof number  $Gr$  and Prandtl number  $Pr$ . The effect of radiation is described by the Stefan-Boltzmann equation

$$Q_{rad} = Ae\sigma(T_0^4 - T_\infty^4) \quad , \quad (7)$$

where  $Q_{rad}$  is the power transferred by radiation,  $e$  is the emissivity of the surface,  $\sigma$  the Stefan-Boltzmann constant,  $T_0$  the absolute temperature of the radiating frame and  $T_\infty$  the absolute ambient air temperature. According to (1) and (7) and the principle of energy-conservation, the governing equation for  $T_0$  yields:

$$\sum_{i=1}^n Q_i = Q_{con} + Q_{rad} = A [e\sigma(T_0^4 - T_\infty^4) + h(T_0 - T_\infty)] \quad , \quad (8)$$

where  $Q_i$  denotes all heat sources within the machine.  $h$  itself is a nonlinear function of  $T_0$ , (3), so that (8) needs to be solved iteratively.

### IV. ELECTROMAGNETIC ANALYTICAL MODEL

Field of application of the analytical model is the design and recalculation process of permanent magnet synchronous machines. The purpose of the developed analytical model is the automated computation of various types of permanent magnet synchronous machines. Therefore, several types of constructions are considered. This includes the winding type, the slot shape and the magnets configuration. Distributed and concentrated windings, five different slot shapes as well as

surface magnets or buried magnets are implemented. Due to the absence of rotor windings and damper circuits, only the voltage equations and stator flux linkage have to be considered. In the rotating coordinate system, used to yield constant mutual reactances and with the assumption  $I_d = 0$ , the following set of steady-state equations is obtained [10]:

$$V_d = R_1 \cdot I_d - X_q \cdot I_q, \quad (9)$$

$$V_q = R_1 \cdot I_q + X_d \cdot I_d + V_p, \quad (10)$$

$$T = \frac{3 \cdot p}{\omega} \cdot V_p \cdot I_q. \quad (11)$$

These are the main equations of the analytical model. The analytic iron loss computation is performed by the, Steinmetz like, formula

$$p_{iron} = k \cdot B^\alpha, \quad (12)$$

where the coefficients  $k$  and  $\alpha$  are determined by loss measurement of 1.0 and 1.5 T, generally provided by steel manufacturer for 50 Hz. On basis of the maximal air gap flux density  $B_o^{max}$  the flux density of stator teeth  $B_{ts}$  and yoke  $B_y$  are estimated. The time-varying flux densities  $B_{ts}$  and  $B_y$  generate the following iron losses

$$P_{teeth} = V_{ts} \cdot \rho \cdot p_{iron}(B_{ts}) \cdot \frac{n \cdot p}{50 \text{ Hz}} \quad (13)$$

$$P_{yoke} = V_y \cdot \rho \cdot p_{iron}(B_y) \cdot \frac{n \cdot p}{50 \text{ Hz}} \quad (14)$$

where  $V_{ts}$  and  $V_y$  are the volumes of the corresponding stator section,  $\rho$  the specific mass density of the laminated steel sheets,  $n$  the actual rotor speed and  $p$  the number of pole pairs.

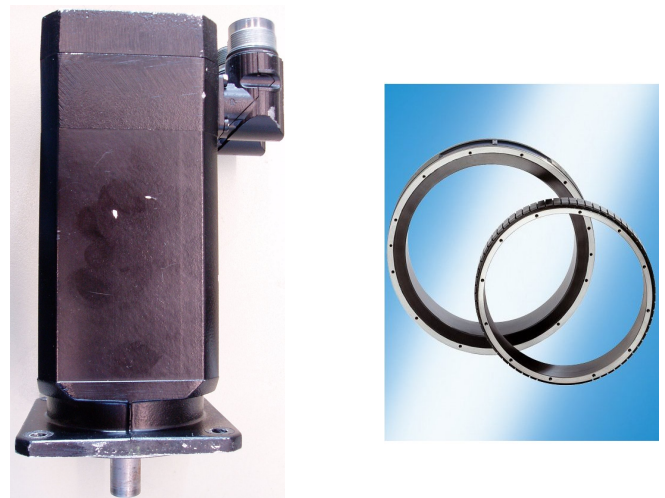
## V. ELECTROMAGNETIC NUMERICAL SIMULATION

The numerical simulation is performed using iMOOSE. This software package consists of solvers for different problem definitions such as static, transient and harmonic problems. For all performed finite element computations in this study the node-based transient FEM solver for 2D electromagnetic field problems with eddy-current regions is employed. Due to the requirements of an automated design process, the problem definition and the mesh must be generated automatically. The mesh generation is controlled by a Python based scripting language, which transcribed a predefined machine model to common CAD file formats. To keep the modeling and meshing process flexible, they are parameterized through the output of the analytical model or directly by the geometrical data. To be independent from the number of pole pairs and stator slots, a complete 360° model is simulated.

## VI. VALIDATION

The presented design tool has been applied to two permanent magnet synchronous machines for industrial applications

in order to validate the concept. In study case A an industrial series PMSM is redesigned on basis of the rated performance data and the geometry specifications. The results are then critically compared to the real geometrical data. Afterwards the results of the electromagnetic simulation and the thermal analysis are compared with measurements. Case B deals with a second shape optimized standard servo drive which requires designated modifications of the automated design process to demonstrate the flexibility of the electromagnetic and thermal model. Both study cases are electrical drives of actual series production, so that, in accordance with non-disclosure agreements, no geometry cross sections or constructions details are given.



(a) PMSM of the **DS56L** type series produced by SEW-EURODRIVE.

(b) **MBT201D-0027** servo-drive, produced by the Bosch-Rexroth Group.

Fig. 3. Pictures of permanent magnet synchronous machines for industrial applications.

### A. Study Case A

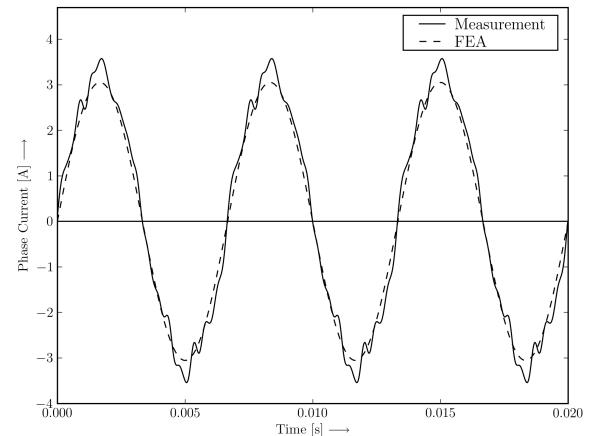
The first study case for validation is a permanent magnet synchronous machine of the **DS56L** type series produced by SEW-EURODRIVE. The dimensioning process is initialized for a rated speed of 3000 rpm and a rated torque of 2 Nm, leading to 628 W rated power. Technical specifications imposed a concentrated winding with a phase voltage of  $\frac{150}{\sqrt{2}}$  V. In accordance with construction-related designations, the stator slot shape is trapezoidal with rounded tooth tips. Moreover, magnet form and characteristic dimensions like, shaft diameter, copper fill factor, air gap height and the ratio of inner stator diameter to active length are specified. On basis of these design parameters, the electrical and geometric dimensioning is performed according to the rules presented in [1]. Table I lists the deviations between computed and actual

cross section characteristic length. The results of the sizing process are in good agreement with the actual dimension of the **DS56L** servo-drive; In order to verify the analytical and

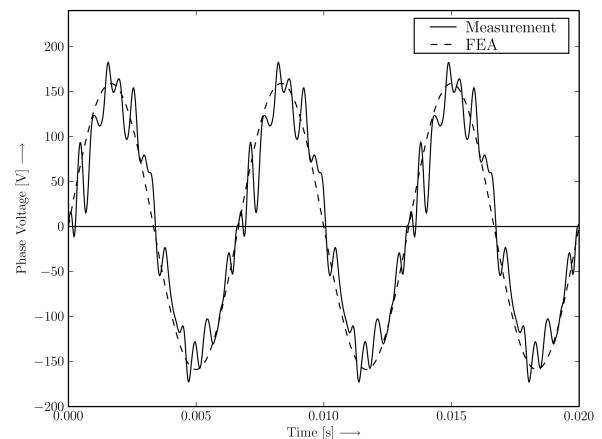
TABLE I  
ABSOLUTE DEVIATION BETWEEN COMPUTED AND REAL CROSS SECTION PROFILE FOR RELEVANT GEOMETRIC PARAMETERS IN MM.

Geometry	Abs. Deviation [mm]
outer stator diameter	2.6
stator yoke height	1
stator tooth width	0.9
stator tooth height	0.34
tooth tip height	0

numerical methods, the virtual design process is continued with the original geometric dimensions of the **DS56L**. Assuming a sinusoidal current excitation, and using (11), the rated working point ( $M= 2 \text{ Nm}$ ,  $n= 3000 \text{ rpm}$ ) is computed by analytic and numeric finite element simulation. In both cases the phase voltage is determined by the electromagnetic steady-state equations (9), (10). Fig. 4(a) shows the measured phase currents in comparison with the assumed sinusoidal current. The corresponding phase voltage provided by measurement and FEA are shown in function of time in Fig. 4(b). Both quantities, phase current and phase voltage, exhibit minor deviation with respect to measurements, which basically results from the assumption of a sinusoidal current excitation. The difference between analytic and numeric electromagnetic simulation is about 0.5 %, so that an additional parameterization by FEA is not required, cf. Fig. 1. The analytical model can be considered having an adequate efficiency, with respect to a finite element analysis, for the computation of various working points. Tab. II compares the computed electric efficiency for the rated torque of 2 Nm in the speed range from 500 rpm to 3000 rpm with measurements. In terms of the presented application concept, a rapid-prototype development, these efficiency results are in good agreement. Fig. 5 illustrates the machine's whole efficiency map, processed by [11]. In preparation for the thermal network model, iron losses in stator teeth and yoke are determined analytically by (13) and (14). Joule losses of the coil and the endwinding are identified by separating ohmic losses according to their proportion in volume. Bearing losses are estimated in function of the rotor speed, whereas eddy current losses were neglected with respect to the machines power and speed. The **DS56L** is a servo-drive with natural convection, so that the average frame temperature  $T_0$  is determined by solving (8) iteratively, with the nonlinear heat transfer coefficient  $h$ , defined by (2) - (6). The left-hand side of (8) is the sum of iron, joule and bearing losses. In case of an ambient air temperature of 23 °C, the solution of (8) gives an average frame temperature of 77 °C, which is in acceptable agreement with a measured



(a) Phase Current



(b) Phase Voltage

Fig. 4. Comparison between the measured and computed quantities phase voltage and phase current.

frame temperature of 70 °C. For the **DS56L** no further thermal measurements were available, so that the estimated temperature of the remaining nodes of the thermal lumped-parameter model could not be validated. The computational thermal results listed in Tab. III show a common and characteristic temperature distribution within the machine parts, which indicate the effectiveness of the thermal model proposed.

### B. Study Case B

As a second example, the automated design process described in section II has been applied to the **MBT201D-0027** servo drive, shown in Fig. 3(b), a high torque direct-drive motor of the IndraDyn T Series of the Bosch-Rexroth

TABLE II  
EFFICIENCY IN FUNCTION OF THE ROTOR SPEED FOR A MOTOR TORQUE OF 2 Nm.

Rotor Speed [1/min]	Simulation %	Measurement %
500	60,77	61
1000	74,66	72
1500	80,7	80
2000	84,02	82
2500	86,07	86
3000	87,44	88

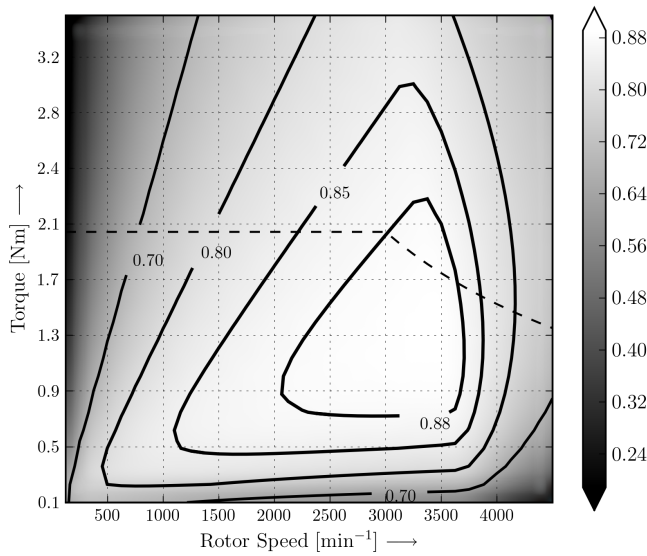


Fig. 5. Efficiency map of DS56L for a power convert with 10 % reserve voltage capacity.

Group. Catalog data sheet are given in Tab. IV. This servomotor has a complicated and optimized geometry, so that the electromagnetic computation is performed numerically by a finite element computation. The whole design process, Fig. 1, is conceived very flexible, so that particular computation blocks can be done analytically, numerically or in parallel to adapt them case by case. Iron losses are determined by a post-processing computation based on the modified Bertotti formula [12] and injected at the corresponding nodes of the thermal network. This machine has an active water cooling system, so that the governing equation for the average frame temperature  $T_0$  by passive heat transfer, (8), can be neglected. In normal operation, thermal measurement states an ingoing coolant temperature of 30 °C and an outgoing cooling fluid temperature of 34 °C. The temperature gradient of the frame along the z-direction can be represented by a mean temperature of 32 °C, which is set as boundary condition for the node  $T_0$  of the thermal equivalent network, Fig. 2.

TABLE III  
RESULTS OF ANALYTIC THERMAL EQUIVALENT NETWORK COMPUTATION OF DS56L FOR AN AMBIENT TEMPERATURE OF 23 °C.

Key Temperature	Computation [°C]	Measurement [°C]
Frame	77	70
Stator Yoke	76	
Stator Teeth	79	
Coil	101	
Endwinding	110	
Magnet	80	
Bearing	78	

All thermal resistivities, except  $R_{th,4}$ , are computed by the provided geometry and material properties according to the general principles described in [7]. The lumped-parameter  $R_{th,4}$ , representing the thermal resistance between stator teeth and the inlaying coil wires, could not be determined analytically due to the uncommon stator shape of the motor. The thermal resistance  $R_{th,4}$  has been varied, so that the simulated endwinding temperature complies with the experiment, see Tab. V. Without further modifications, the simulated and measured temperature in the magnets are identical, which indicates that the governing equations for the concentrated thermal resistances, representing complex machine parts, are reliable and applicable for standard geometries. Furthermore the parameterization of  $R_{th,4}$  exhibits, that empirical investigations or knowledge databases are important for thermal modeling.

TABLE IV  
DATA SHEET OF MBT201D-0027.

rated value	numerical value
Torque $M_n$	140 Nm
Speed $n_n$	330 $\text{min}^{-1}$
Power $P_n$	4,84 kW
Voltage $U_n$	366 V
Current $I_n$	13 A

TABLE V  
RESULTS OF ANALYTIC THERMAL EQUIVALENT NETWORK COMPUTATION OF MBT201D-0027 FOR AN AVERAGE FRAME TEMPERATURE OF 32 °C.

Key Temperature	Computation [°C]	Measurement [°C]
Stator Yoke	37	–
Stator Teeth	67	–
Coil	114	–
Endwinding	131	130
Magnet	74	74
Bearing	80	–

## VII. DISCUSSION

The proposed automated design process for permanent magnet synchronous machines, regarding electromagnetic and thermal aspects, cf. flowchart 1, is implemented, by means of modern object-oriented programming, resulting in a flexible and multifunctional development process. The independent computation blocks, such as dimensioning, analytic and numeric electromagnetic model, thermal equivalent network and numerical finite element analysis, are combined sequentially by appropriate data structures. Iterations can be performed automatically or directly by a user interaction. If required, single blocks can be skipped, adapted or modified. Necessary results in the subprocesses, required to complete the whole process, can be provided by equivalent types of computation, e.g. analytic or numeric situations, or the user itself. This proceeding is exemplified in study case B, see section VI-B, where the analytic electromagnetic simulation is directly replaced by FEA to analyze a geometry optimized servomotor. Additionally the geometric data has been specified, not determined by the sizing process. The results of the equivalent thermal network simulation are in agreement with measurements, and exhibit the characteristic temperature distribution. This demonstrates the practicability and flexibility of the applied analytic thermal model, but case B shows some inherent limitations of this kind of approaches. For uncommon and complex geometry shapes classical analytic formula for individual thermal resistances are misleading, and resorting to empiric data or other feasible approaches, e.g. a parameterization by thermal finite-element method is required.

## VIII. CONCLUSIONS

The consideration of thermal phenomena is essential in the PMSM sizing process. Even if analytical thermal models estimate only the temperature at characteristic points of electrical machines and are not as detailed as whole FEA temperature distributions, it is worth seeking approximative models capable for rapid design processes. The presented approach extends the FEA parameterized electromagnetic dimensioning model of [1], with a thermal lumped-parameter model to consider thermal effects on the sizing process and the electromagnetic behavior. The whole design process is demonstrated with two standard industrial servo-motors for passive and active water cooling. The redesign of one motor by the sizing process, on basis of classical design parameters, shows minimal deviations in the resulting geometric dimensions. Electromagnetic FEA results, performed for both test machines, are compared to the measured quantities phase voltage and phase current. In case of standard geometry the utilized electromagnetic analytic model gains a sufficient accuracy with respect to measurement and FEA. Losses, obtained analytically, numerically or as combination of both, are injected as excitations in the

automatically generated equivalent thermal network. Thermal measurements are compared with the estimation of the thermal model, showing its capability for standard geometries, but an inherent weakness for individual, nonstandard shapes. Further investigations are necessary to clarify which methods are appropriate to provide adequate data in that case and can be integrated into the design process. Moreover the thermal equivalent model has shown to be very flexible and is also applicable to machines equipped with forced convection cooling systems [13].

## IX. ACKNOWLEDGEMENT

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## REFERENCES

- [1] M.Schöning and K.Hameyer, "Coupling of analytical and numerical methods for the electromagnetic simulation of permanent magnet synchronous machines," *Journal for Computation and Mathematics in Electrical Engineering (COMPEL)*, vol. 27, no. 1, 2008.
- [2] M.Schöning and K. Hameyer, "Applying virtual reality techniques to finite element solutions," *IEEE Transactions on Magnetics*, 2008.
- [3] D.van Riesen, C.Monzel, C.Kaehler, C.Schlensok, and G.Henneberger, "iMOOSE-an open-source environment for finite-element calculations," *IEEE Transactions on Magnetics*, vol. 40, no. 2, pp. 1390-1393, 2004.
- [4] M.Schöning, E.Lange, and K.Hameyer, "Development and validation of a fast thermal finite element solver," ICEM, 2008.
- [5] G.van Rossum, "The python programming language," 2008. [Online]. Available: <http://www.python.org/>
- [6] T.Oliphant, "Scipy-scientific tools for python," 2008. [Online]. Available: <http://www.scipy.org/SciPy>
- [7] J.Lindström, "Thermal model of a permanent-magnet motor for a hybrid electric vehicle," Department of Electric power Engineering, Chalmers University of Technology, Göteborg, Sweden, Tech. Rep., Apr. 1999.
- [8] A.M.El-Refaei, N.C.Harris, T.M.Jahns, and K.M.Rahman, "Thermal analysis of multibarrier interior pm synchronous machine using lumped parameter model," *IEEE Transactions on Energy Conversion*, vol. 19, no. 2, pp. 303-309, Jun. 2004.
- [9] VDI-Gesellschaft Verfahrenstechnik und Chemieingenieurwesen, *VDI Wärmeatlas*, 10th ed. Berlin: Springer, 2006.
- [10] P.Vas, *Vector Control of AC Machines*. Oxford: Clarendon Press, 1990.
- [11] "Matplotlib, A plotting library for the Python programming," online, 2008. [Online]. Available: <http://matplotlib.sourceforge.net>
- [12] M. Herranz Gracia, E. Lange, and K. Hameyer, "Numerical calculation of iron losses in electrical machines with a modified post-processing formula," in *16th Conference on the Computation of Electromagnetic Fields*, 2007.
- [13] J.R.Hendershot Jr and T.Miller, *Design of Brushless Permanent-Magnet Motors*, 2nd ed. Walton Street, Oxford OX2 6DP: Oxford University Press, 1994.
- [14] "Bosch Rexroth AG," online, 2008. [Online]. Available: <http://www.boschrexroth.com>
- [15] "SEW-EURODRIVE," online, 2008. [Online]. Available: <http://www.sew-eurodrive.de>